



Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

Sustainable intergenerational preferences

Combining sensitivity for the interests of the present with respect for the interests of the future

Geir B. Asheim

University of Oslo

International Conference on
Science and Technology for Sustainability 2008
In Search of Sustainable Well-Being
Tokyo, 12-13 September 2008



Brundtland commission's definition of sustainability

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Outline

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

“Believing that **sustainable development**, which implies *meeting the needs of the present without compromising the ability of future generations to meet their own needs*, should become a central guiding principle of the United Nations, Governments and private institutions, organizations and enterprises”

- Points to a conflict between the interests of the **present** and the interests of **future** generations
- But does not indicate how this conflict should be resolved



Three different problems

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Outline

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

- 1 Clarifying the concept of individual well-being (as discussed in Professor Pattanaik's keynote address)
- 2 Aggregating individual well-being into a concept of aggregate well-being for one generation
- 3 Aggregating generational well-being into a measure that can be used for evaluating policies that have intergenerational effects

Utility will refer to a specific cardinal scale for generational well-being and a *utilitarian criterion* will make use of such a scale



Outline

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction
Outline

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

- Discuss how various criteria for intergenerational equity
 - discounted utilitarianism
 - **undiscounted utilitarianism**
 - **ordinary/lexicographic maximin**
- fail to take into account the interests of both present and future generations
- *Alternative I: Sustainable preference* (Chichilnisky, 1996)
 - *Alternative II: Sustainable recursive social welfare function* (Asheim, Mitra and Tungodden, 2008)
 - *Special case: Sustainable discounted utilitarianism* (Asheim and Mitra, 2008) Illustrate how this criterion takes into account the interests of both the present and the future



Failure of established criteria

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Disc. util.
Undisc. util.
Maximin

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

- Discounted utilitarianism
- Undiscounted utilitarianism
- Ordinary/lexicographic maximin



The failure of discounted utilitarianism

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Disc. util.
Undisc. util.
Maximin

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

- Maximize the sum of utilities discounted at a positive rate
- Positive utility discounting entails that generations are treated in an unequal manner

Consequence in growth models

In the [Dasgupta-Heal-Solow-Stiglitz](#) model of capital accumulation and resource depletion, it forces consumption to approach zero as time goes to infinity, even though sustainable streams with constant or increasing consumption are feasible



Consequence in the DHSS model

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Disc. util.
Undisc. util.
Maximin

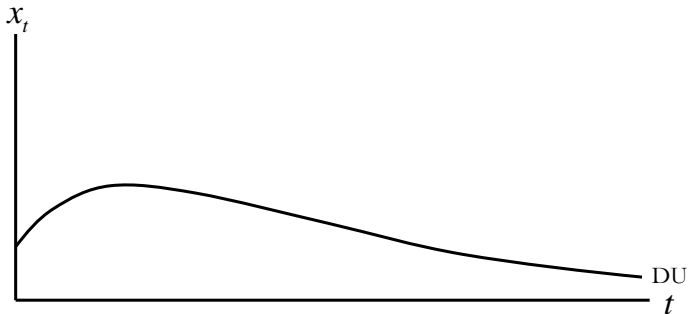
Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms





The failure of discounted utilitarianism

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Disc. util.
Undisc. util.
Maximin

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

Resolving the conflict between the present and the future

Well-being



The black stream might be preferred



The failure of undiscounted utilitarianism

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Disc. util.
Undisc. util.
Maximin

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

- Maximize the undiscounted sum of utilities
- It demands that the present make sacrifices for the future

Consequence in growth models

In the one-sector [Ramsey](#) model
and in the [Dasgupta-Heal-Solow-Stiglitz](#) model
of capital accumulation and resource depletion,
it results in consumption growth beyond all bounds, thereby
leading to gross inequalities between the present and the future



Consequence in the DHSS model

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Disc. util.
Undisc. util.
Maximin

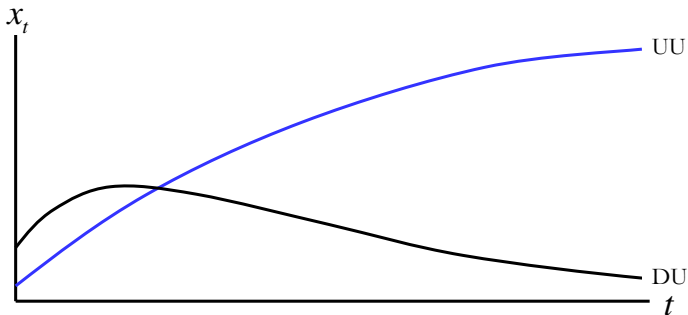
Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms





The failure of undiscounted utilitarianism

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Disc. util.
Undisc. util.
Maximin

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

Resolving the conflict between the present and the future



The blue stream is always preferred



The failure of ordinary/lexicographic maximin

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Disc. util.
Undisc. util.
Maximin

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

- Maximize the well-being of worst-off generation
- It does not allow trading off the interests of the present for the benefit of future prosperity

Consequence in growth models

In the one-sector [Ramsey](#) model
and in the [Dasgupta-Heal-Solow-Stiglitz](#) model
of capital accumulation and resource depletion,
it does not permit growth and development,
thereby perpetuating poverty



Consequence in the DHSS model

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Disc. util.
Undisc. util.
Maximin

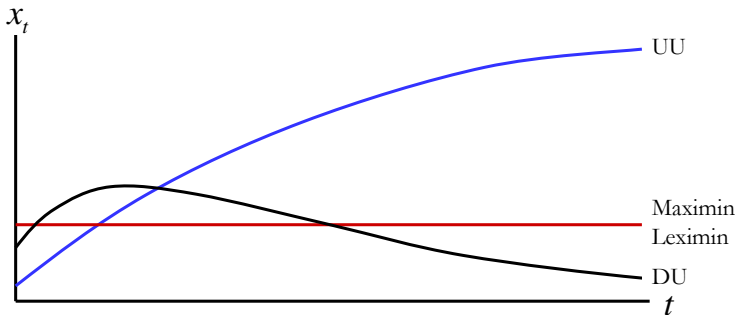
Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms





The failure of ordinary/lexicographic maximin

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Disc. util.
Undisc. util.
Maximin

Sustainable
preference

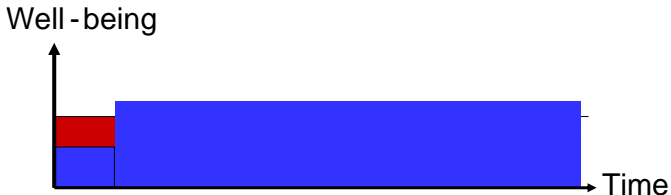
Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

Resolving the conflict between the present and the future



The blue stream is never preferred



Sustainable preference

Chichilnisky SCW (1996)

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference
Existence and
properties

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

- **Numerically representable social welfare function**

Not satisfied by **Undiscounted utilitarianism**

Not satisfied by **Lexicographic maximin**

- **Strong Pareto (SP):**

Sensitivity for the interests of each generation

Not satisfied by **Ordinary maximin**

- **No Dictatorship of the Present (NDP):**

Not that only what happens before a finite T matters

Not satisfied by Discounted utilitarianism

- **No Dictatorship of the Future (NDF):**

Not that only what happens beyond a finite T matters



Existence and properties of a Sustainable preference

Sustainable intergenerational preferences

Geir B. Asheim

Introduction

Failure of established criteria

Sustainable preference
Existence and properties

Sustainable recursive SWF

Sustainable disc. utilitarianism

Conclusion

Axioms

The following social welfare function is a sustainable preference:

$$\alpha \underbrace{\left((1 - \delta) \sum_{t=0}^{\infty} \delta^t U(x_t) \right)}_{\text{Discounted utilitarianism}} + (1 - \alpha) \underbrace{\liminf_{t \rightarrow \infty} U(x_t)}_{\text{Depends on the infinite future}}$$

- Does not satisfy **Independent Future (IF)**
Lead to time-inconsistent optimal streams
- Non-existence of optimal streams in growth models
No optimal stream in the one-sector [Ramsey](#) model and in the [Dasgupta-Heal-Solow-Stiglitz](#) model of capital accumulation and resource depletion



Consequence in the DHSS model

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

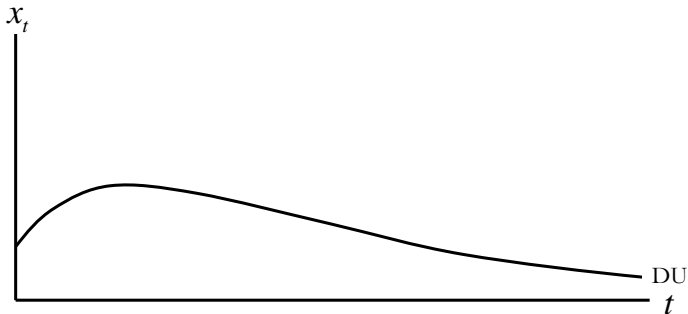
Sustainable
preference
Existence and
properties

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms





Sustainable recursive social welfare function

Asheim, Mitra and Tungodden (2008)

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Existence and
properties

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

- **Order (O):** *A complete and transitive binary relation*
- **Monotonicity (M):** *More is not worse*
- **Restricted Dominance (RD)**
- **Independent Future (IF):**
Future choice does not depend on present well-being
Not satisfied by **Ordinary maximin**
- **Hammond Equity for the Future (HEF):**
Priority for the future if the present is better off
Not satisfied by Discounted utilitarianism
- **Restricted Continuity (RC):** *Supnorm continuity when approaching a stream with constant future well-being*
Not satisfied by **Undiscounted utilitarianism**
Not satisfied by **Lexicographic maximin**



Existence and properties of a Sustainable recursive SWF

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Existence and
properties

Sustainable
disc. utili-
tarianism

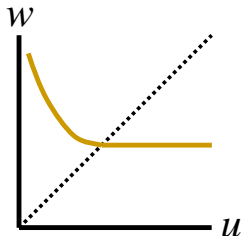
Conclusion

Axioms

Exists a *utility function* U and an *aggregator function* V s.t.

$$W(x, x, x, \dots) = U(x)$$

$$W(x_0, x_1, x_2, \dots) = V(U(x_0), W(x_1, x_2, x_3, \dots))$$





Properties of a sustainable recursive SWF

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Existence and
properties

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

Resolving the conflict between the present and the future



The black stream is never preferred



Properties of a sustainable recursive SWF

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

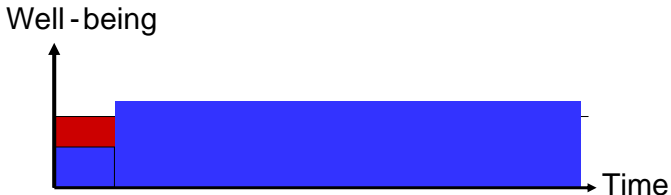
Existence and
properties

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

Resolving the conflict between the present and the future



The blue stream is sometimes preferred

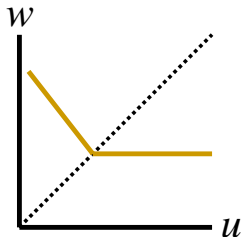


Special case: Sustainable disc. utilitarianism

Asheim and Mitra (2008)

Departs from DU by requiring that the SWF be insensitive to the interests of the present if the present is better off than the future

$$W(x_0, x_1, x_2, \dots) = \begin{cases} (1 - \delta)U(x_0) + \delta W(x_1, x_2, x_3, \dots) & \text{if } U(x_0) \leq W(x_1, x_2, x_3, \dots) \\ W(x_1, x_2, x_3, \dots) & \text{if } U(x_0) > W(x_1, x_2, x_3, \dots), \end{cases}$$



Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Existence and
properties

Conclusion

Axioms



Existence and properties of a Sustainable discounted utilitarian SWF

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Existence
and
properties

Conclusion

Axioms

- General existence of a Sustainable disc. utilitarian SWF
- Satisfies **(O)**, **(M)**, **(RD)**, **(IF)**, **(HEF)** and **(RC)**
⇒ Special case of a Sustainable recursive SWF
- Appealing optimal streams in growth models
Optimal stream in the [Dasgupta-Heal-Solow-Stiglitz](#) model of capital accumulation and resource depletion allows for growth and development initially when the economy is highly productive, while protecting the future from the grave consequences of discounting when resource depletion and capital accumulation undermines capital productivity



Consequence in the DHSS model

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

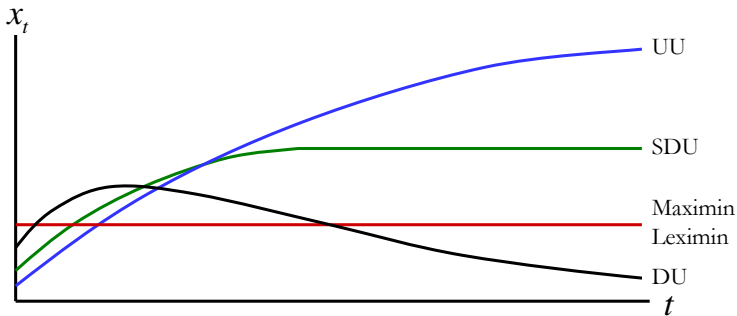
Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Existence and
properties

Conclusion

Axioms





Global warming and intergenerational equity

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

- **The effects of global warming are uncertain**
Perhaps future generations will be able to adapt
Or perhaps future productivity will be undermined
- **State-dependent utility discounting**
Perhaps we wish to (in effect) discount the future less
if future productivity is undermined, to ensure
the livelihood of generations in the far future
- **A purpose of this research**
To show existence of and characterize classes of social welfare functions that allow for such discounting



Global warming and intergenerational equity

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

- **The debate in the wake of the Stern Review** has been limited to what parameters to use in a(n) (un)discounted utilitarian criterion
- **This research shows that** that there is a wider set of criteria for intergenerational equity that should perhaps be considered for evaluating climate policies and policies for sustainable development



Axioms

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

SP
RD
IF
HEF

- Strong Pareto (SP)
- Restricted Dominance (RD)
- Independent Future (IF)
- Hammond Equity for the Future (HEF)



Strong Pareto (SP)

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

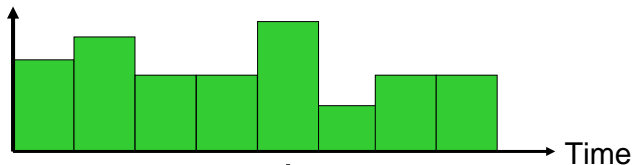
SP

RD

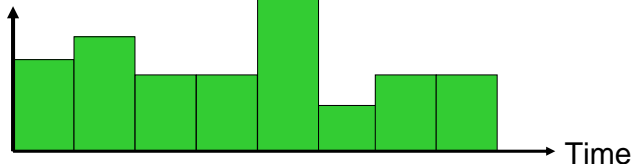
IF

HEF

Well-being



Well-being



The lower stream is preferred



Restricted Dominance (RD)

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

SP

RD

IF

HEF

Well-being



Well-being



The lower stream is preferred



Independent Future (IF)

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

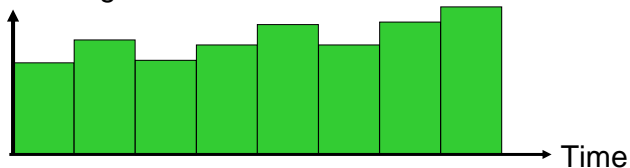
SP

RD

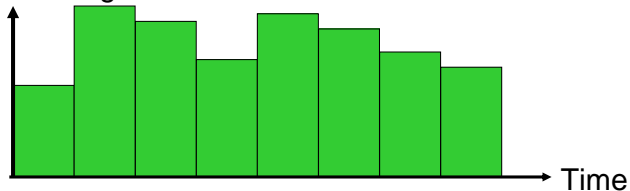
IF

HEF

Well-being



Well-being



If the top is as good as the bottom, ...



Independent Future (IF)

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

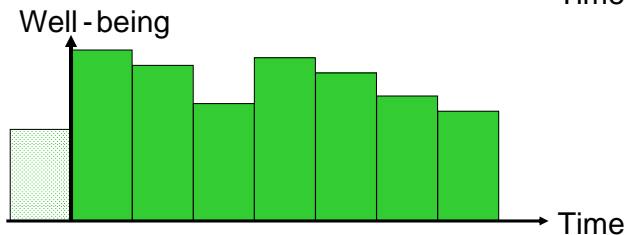
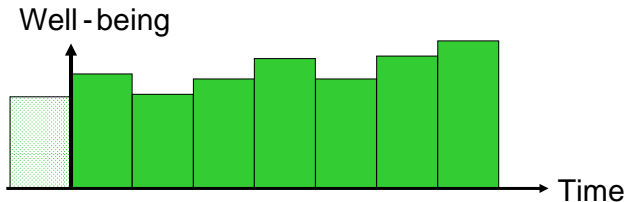
Axioms

SP

RD

IF

HEF



then the top is still as good after the first period



Hammond Equity for the Future (HEF)

Sustainable
intergenerational
preferences

Geir B.
Asheim

Introduction

Failure of
established
criteria

Sustainable
preference

Sustainable
recursive
SWF

Sustainable
disc. utili-
tarianism

Conclusion

Axioms

SP

RD

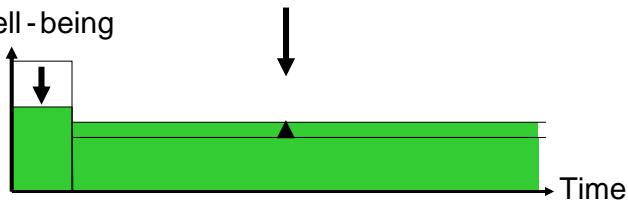
IF

HEF

Well-being



Well-being



The upper stream is not preferred